Resistivity study of the pseudogap phase for (Hg,Re)-1223 superconductors

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The pseudogap phase above the critical temperature of high- T_c superconductors (HTSC) presents different energy scales and it is currently a matter of intense study. The complexity of the HTSC normal state requires very accurate measurements with the purpose of distinguishing different types of phenomena. Here we have performed systematically studies through electrical resistivity (ρ) measurements by several different current densities in order to obtain an optimal current for each sample. This approach allows us to determine reliable values of the pseudogap temperature $T^*(n)$, the layer coupling temperature between the superconductor layers $T_{LD}(n)$, the fluctuation temperature $T_{scf}(n)$, and the critical temperature $T_c(n)$ as a function of the doping n. The interpretation of these different scales allows us to characterize possible scenarios for the (Hg,Re)-1223 normal state. This method, described in detail here, and used to derive the (Hg,Re)-1223 phase diagram is general and can be applied to any HTSC.

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I. INTRODUCTION

One of the greatest puzzles of condensed matter physics is to understand the superconducting fundamental interactions of high- T_c superconductors (HTSC) and their many unconventional properties. Among these, the pseudogap region below T^* and above T_c , the so-called pseudogap phase¹ has attracted a lot of attention in order to determine its precise values as functions of the doping level n and, above all, to understand its nature and its relation to the superconducting phase. Therefore, a large number of different techniques have been used to study the dependence of T^* for many families of compounds.^{1,2} However, the major problem is that the values of T^* differ strongly for different techniques and even a given method may yield different values. In many cases, different temperatures or energy scales are identified in the normal phase,³ which makes it extremely difficult to precisely understand the nature of this phase. Thus, one can find in the literature some different phase diagrams for HTSC. As concerns its nature, many theoretical explanations have been proposed but they can be roughly classified in two main proposals. One is based on the fluctuation of Cooper pairs between T_c and T^* with a nonvanishing order parameter without phase coherence or long range order.⁴ The other proposal is based on the existence of some other type of order which may compete with the superconducting order.^{2,5–7}

We attempt here to define a systematic approach to study the pseudogap phase. Among the many different techniques used to solve this problem,^{1,2} transport properties by electrical resistivity measurements have been considered one of the most useful ones. At high temperatures, the resistivity (ρ) has a linear behavior with the temperature and T^* is defined as the temperature in which $\rho(T)$ starts to decrease below such linearity. However, it is well known that there are considerable differences in the values of T^* found in some published works.^{8–12} It is very likely that the discrepancy at T^* has its origin in the fact that there are many parameters, which can determine the accuracy of the resistivity measurements. As considering polycrystalline samples, these factors are the morphology of the junctions, the cross section of the grains, and stoichiometry in the grain.¹³ However, the most important factor is the applied current density value and its influence on the resistivity measurements in polycrystal or single crystal. In order to obtain precise values of T^* , it is crucial to perform the measurements in the linear or low current regime but, if the current is too low, the values could be plagued by high noise. Therefore, the precision of resistivity measurements is an open question: What would be the ideal current applied to a polycrystalline sample? A search in the literature shows that there is no consensus about what is the ideal value to be used at the four-point probe, and as will be discussed below, they differ by several orders of magnitude in the literature.

In this paper, we outline a method in which the values of the voltage V=V(I) and $\rho(T)$ are measured by several values of current I and temperature T, in order to find a range of current density that is ideal to determine T^* . In simple terms, we search for the maximum current density value that is in the limit of linear response. So far as we know, there is not any published systematic analysis of this type despite its importance. Taking advantage of the precision of our data we also discuss the Lawrence-Doniach (LD) temperature criteria generalized by Klemn¹⁴ in the case of several superconducting layers in a periodicity length.¹⁵ The analysis of the T_{LD} is very interesting because it gives a feeling of the superconducting coupling among the layers. We have also used these data to discuss the thermodynamic fluctuations of the Cooper pairs through the phase fluctuation temperature T_{scf} ,¹⁶ which is important to the discussion of the pseudogap scenario. This paper is organized as follows: in Sec. II we discuss the experimental details of sample preparation, characterization, and resistivity measurements. In Sec. III we describe our systematic study of the applied current linear regime. We discuss how to calculate T^* , T_{LD} , and T_{scf} . These temperatures together with T_c provide a possibility to discuss the phase diagram.

II. EXPERIMENTAL DETAILS

A. Superconductor synthesis

The ceramic precursor preparation protocol began with a mixture of $Ba_2Ca_2Cu_3O_x$ (99.0% PRAXAIR) and ReO_2 (99.0% Aldrich) in powder form with the molar relationship 1:0.18.¹⁷ These powders were homogenized, pelletized, and heated at 850 °C in a flow of oxygen (99.5% purity) for 15 h. The obtained precursor was crushed, homogenized, and compacted again before being heated a second time at 920 °C for 12 h in a flow of oxygen. The later procedure is repeated for seven more times to provide a good homogenization,¹⁸ as discussed in more detail in a previous work.¹⁷

The precursor material was submitted to an annealing at 920 °C for 24 h in a flow of a gas mixture of argon (99.5% purity) and oxygen (99.5% purity) maintained at 1 bar. Three different ceramic precursors were prepared with distinct partial pressure of oxygen PO₂: 5% of O₂ and 95% of Ar (sample *A*), 10% of O₂ and 90% of Ar (sample *B*), and 15% of O₂ and 85% of Ar (sample *C*).^{17,19}

Finally, the three precursors prepared with different PO₂ were blended with HgO at a molar relationship 1:0.82, homogenized and palletized. The pellets with typical dimensions $5 \times 5 \times 20 \text{ mm}^3$ were wrapped in a gold foil (99.999%) and introduced in a quartz tube with 8 mm inner diameter. Each sample (*A*, *B*, and *C*) wrapped with a gold foil has received an excess of Hg (l) in amalgam form. The ratio between the mercury mass and the gold mass was 0.045. Based on the study of the quartz tube filling factor effect (ff), it was used ff $\approx 1.0 \text{ g cm}^{-3}$ and ff_{Hg} $\approx 0.010 \text{ g cm}^{-3}.^{20}$ The quartz tubes were sealed in a high vacuum of 3×10^{-6} torr and were submitted to 72 h of annealing time at 865 °C.^{13,17,19}

B. Superconductor characterization

1. X-ray diffraction measurements

X-ray diffraction (XRD) analysis with Rietveld refinement was done in *A*, *B*, and *C* samples with the purpose of completing the Orlando *et al.*¹⁷ study. The XRD measurements were performed using laboratory diffractometer models Rigaku Multiflex and D-MAX with Cu $K\alpha$ radiation. In order to complete the investigation, x-ray diffraction mea-



FIG. 1. Rietveld plot of sample A (underdoped). The spectrum was plotted in a range from 20° up to 120° . The insert shows a 001 peak (5° up to 6°) and the convolution of two phases at 8950 eV.

surements were carried out in the x-ray powder diffraction beam line, D10B-XPD, of the Brazilian Synchrotron Light laboratory (LNLS), located in Campinas, SP, Brazil. Two different energies were used to perform the experiments: 8950 and 10600 eV. The first energy is similar to Cu $K\alpha$ radiation and the second one was chosen 65 eV after the rhenium edge L_{III} , where the rhenium scattering factor is higher than in 8950 eV (anomalous x-ray scattering). For all measurements the spectra were performed from 2° up to 122° with 0.01° step scan. In the case of laboratory diffractometers the counting time varied from 15 up to 25 sec, using very narrow slits to limit the x-ray beam. For the synchrotron light measurements the variable counting time statistics took into account the decrease of the beam current in the LNLS storage ring. The instrumental parameters were obtained from the refinement of standards LaB₆ and Al₂O₃ (NIST standard reference materials) samples. Rietveld refinements²¹ were performed using the program GSAS (Ref. 22) with the interface EXPGUI.²³

A typical Rietveld plot is shown in Fig. 1. For each XRD pattern, the better spectrum fit was obtained including an extra Hg-1223 phase additionally to the main (Hg,Re)-1223 phase, as compared to our previous work.¹⁷ All refinements have considered the following phases: (Hg,Re)-1223 (rich in oxygen) and Hg-1223 (poor in oxygen), HgCaO₂, BaCO₃, CaCuO₂, and BaCuO₂.^{24,25} The main (Hg,Re)-1223 and Hg-1223 phases, their fitted parameters, and the goodness-of-fit are shown in Table I.²⁵ The existence of two superconducting phases was first detected by anomalous x-ray diffraction carried out at 8950 and 10 600 eV at the Brazilian Synchrotron Light Source (LNLS)—Campinas—Brazil.^{26,27} Moreover, it was confirmed by anomalous x-ray diffraction that Re distribution on the Hg-O plane did not produce a supercell $(2a \times 2b \times 1c)$ in any sample (*A*, *B*, and *C*).^{25,27}

The main (Hg,Re)-1223 phase was very crystalline as considering small broadening of their peaks. Besides, the crystallite average sizes were determined from the pseudovoigh profile coefficients of the Le Bail fitting, using the formalism of Steffens,^{22,28} Thompson approach,²⁹ and the Finger asymmetry correction.³⁰

	Parameter	Sample A	Sample B	Sample C
	% (Hg,Re)-1223	61.4	68.7	50.3
	% Hg-1223	26.1	24.7	40.8
Phase 1	<i>a</i> (Å)	3.854516(14)	3.854120(12)	3.854382(16)
	<i>c</i> (Å)	15.687440(40)	15.688061(56)	15.689091(70)
	<i>l</i> (Å)	>1000	>1000	>1000
Phase 2	<i>a</i> (Å)	3.854295(18)	3.853526(15)	3.854320(10)
	<i>c</i> (Å)	15.698784(60)	15.701567(65)	15.692780(76)
	<i>l</i> (Å)	590	380	470
	χ^2	1.465	1.882	1.496
	Rwp (%)	3.83	3.03	3.70

TABLE I. Results of the Le Bail fifs and crystallite sizes obtained from the XRD profile breadths. The Hg,Re-1223 and Hg-1223 phases are labeled by phase 1 and phase 2, respectively.

For all samples the estimated crystallite size to the (Hg,Re)-1223 phase was larger than the range measurable by this method ($l \sim 1000$ Å). This indicates that during the final step of the synthesis a strong growth of crystallites occurs. On the other hand, the extra Hg-1223 phase has smaller crystallite as shown in Table I. Both phases did not present microstrains.

2. SEM and EDS analysis

As described in Ref. 13, the precursor annealing influenced the oxygen partial pressure inside the sealed quartz tube. For the phase diagram region PO₂ < 0.2 bar, the effect of the PO₂ pressure on the junction crystal size has been analyzed since 2000. With this aim in mind, we have obtained scanning electron microscopy (SEM) images. Using the image of sample A (see Fig. 2), a histogram of the grainboundary size was done.¹³ This procedure was also used for samples B and C. From these SEM images, the average junc-



FIG. 2. SEM image performed on sample *A* (underdoped). It can observe that the randomly oriented grain array, which is typical of a polycrystalline compound.

tion sizes $\langle L \rangle$ were determined³¹ and are shown in Table II. In addition, an energy dispersion x-ray spectra (EDS) analysis was done. These measurements have indicated the stoichiometry of the Hg, Re, Ba, Ca, and Cu elements present in the three samples. It was shown in the micrographs as a gradient in the content of Re from the center to the boundary of the particle.¹³ In our point of view, the Hg-1223 phase is preferentially formed in the periphery of the grains as a shell in which the crystallites were smaller than the center. Summarizing, the samples have similar morphology of the grains, average junction sizes, and the same junction type (superconductor-insulate-superconductor), as reported in our recent work.³¹

3. ac susceptibility measurement

The intergrain region of samples was investigated by an ac magnetic susceptibility (χ_{ac}) using these samples in pellet form. Figure 3 shows the χ'_{ac} and χ''_{ac} components under distinct magnetic field (0.075, 0.20, 2.0 Oe) for sample *B*. In general, the out-of-phase component χ''_{ac} displays two peaks at distinct temperatures. The first is small and located close to T_c , and it is related to the intragrain-intrinsic-superconducting transition, which represents the statistical average bulk properties inside each grain of ceramic. The first, and its shape depends on the characteristic intergrain connectivity (weak link region) of the grains in the superconductor ceramic sample.³² The in-phase component χ'_{ac} of the

TABLE II. Sample composition obtained by EDS measurements. The value $\langle L \rangle$ is the average junction size of the grain carried out by a SEM image analysis.

Sample	Grain	$\left< L \right> (\mu \mathrm{m})$
A	Hg _{0.83} Re _{0.17} Ba _{1.98} Ca _{2.01} Cu _{2.98} O _{8+δ}	2.1
В	$Hg_{0.80}Re_{0.20}Ba_{1.99}Ca_{2.00}Cu_{2.98}O_{8+\delta}$	2.7
С	$Hg_{0.79}Re_{0.21}Ba_{2.03}Ca_{1.98}Cu_{2.99}O_{8+\delta}$	2.4



FIG. 3. ac magnetic susceptibility measurements presenting χ' real part and χ'' imaginary part for sample *B*. The measurements were performed under distinct magnetic field at ν =43 Hz.

ac susceptibility presented two transitions towards lower diamagnetic screening.

The T_c criterion was defined as the point where the χ'_{ac} signal is twofold the average noise value, which was measured before the superconductor transition.¹⁷ All details of the measurement procedures were reported elsewhere.¹³ The onset critical temperatures T_c for the (Hg,Re)-1223 phase were (132.6±0.2) K, (133.2±0.2) K, and (132.7±0.2) K for samples A, B, and C, respectively. The χ_{ac} measurements were repeated on the same samples in powder form (38 μ m), and it was also yielded the same T_c .¹³

For the Hg-1223 phase, the onset critical temperature T_c was taken at a cusp of a χ_{ac}'' imaginary signal using magnetic field amplitude H_a =0.075 Oe and ν =43 Hz. The T_c values found in these conditions were (127.0±1) K, (129.5±1) K, and (127.0±1) K. As intergrain morphologies are similar, the different T_c is attributed to the Hg-1223 phase present in the grain boundary. The exam of lattice parameters for the Hg-1223 phase (Table I) reveals that this phase is underdoped and the expected T_c would be (120±3) K, (124±3) K, and (120±3) K for samples A, B, and C, respectively, considering Ref. 33. Therefore, from room temperature to 130 K the Hg-1223 phase is in normal state (nonsuperconductor).

The results suggest that the (Hg,Re)-1223 phase has similar oxygen contents, that is, alike physical properties for the samples were expected. Our conclusion is that the rhenium doping is a main oxygen fixing mechanism in the (Hg,Re)-1223 compound. The Re atom provides extra oxygen atoms in the HgO_{δ} planes.^{17,34} For the Hg-1223 (without rhenium), the oxygen is found at the $(\frac{1}{2}, \frac{1}{2}, 0)$ are responsible for the doping variation since they are loosely bond to the Hg atoms. This mechanism leads to an easy intercalation or removal of the oxygen during the synthesis. However, in the (Hg,Re)-1223 phase, there is a stronger Re-O bond, which has presented an oxygen at (0.33, 0.33, 0).¹⁷ The Re atom has also added or removed an extra oxygen in the crystallographic site $(1, \frac{1}{2}, 0)$ or $(\frac{1}{2}, 1, 0)$. Therefore, the oxygen in the Re-O bond present in 20% of the sample would be unlike the oxygen in the Hg-O bond and it may not be removed with a lower oxygen partial pressure present in the synthesis process.

Sin *et al.*³⁵ have shown the phase diagram of (Hg,Re)-1223 as a function of the oxygen partial pressure (PO₂) of the precursor. For a precursor prepared with PO₂ \leq 0.2 bar, it was found a high (Hg,Re)-1223 phase content and a slightly T_c parabolic variation. On the other hand, it was shown in our previous paper^{13,17} that the T_c value has not enough parameter to define the oxygen contents in (Hg,Re)-1223 phase.

It was already observed that the ac susceptibility measurement under external hydrostatic pressure is an important tool to confirm a small difference in oxygen doping. The samples in powder form have presented distinct dT_c/dP values (8 ± 1) , (1.9 ± 0.2) , and (-1.6 ± 1) K/GPa, which was associated with underdoped, optimaldoped, and overdoped oxygen contents, respectively.¹³ In recent work,¹⁷ we have reported thermopower measurements that confirmed and determined the oxygen content in each sample.

4. Resistivity setup measurements

The dc electrical resistance of the samples was measured using the four-point probe method. The samples were cut in slab form with dimensions of $1.2 \times 1.0 \times 7.0$ mm³ and they were fixed on a sapphire sample holder by using General Electric GE 7031 varnish. The four contacts with low electric resistance (5±1 Ω) were attached to the samples with silver paint. A Keithley 228A Current Source applied currents form 0.4 up to 10 mA at a fixed temperature, and the corresponding voltage values were obtained using a KEITHLEY 182 sensitive digital voltmeter.

The *I-V* curves were measured reversing the current direction during measurement in order to avoid contact resistance influence. The temperature was measured by a copperconstantan thermocouple attached to the sapphire and linked to the HP 34401A multimeter. A PC computer by IEEE-488 interface recorded all data.

III. ELECTRICAL RESISTIVITY ANALYSIS

A. Pseudogap temperature

A search in the literature reveals that there is no consensus about what is the ideal current that must be used at the four-point probe, however it is crucial to be in the linear regime in order to calculate T^* . For instance, in the case of thin films, Qiu et al.36 have applied a current of 0.01 mA ($J \simeq 1.5$ A/cm²). Wuyts *et al.*¹¹ have measured the temperature dependence of the resistivity with a current density $J \le 10^2$ A/cm². For polycrystalline samples, Jover et al.³⁷ have used a current of 1.8 mA, while Batista-Leyva et al.³⁸ have used 0.35 mA. González et al.³⁹ have measured the resistivity within the linear response regime with a current density of 0.07 A/cm² applied to the $Hg_{0.82}Re_{0.18}Ba_2Ca_2Cu_3O_{8+d}$ sample or (Hg,Re)-1223 sample. In addition, Palstra et al.⁴⁰ have checked the linearity of the I-V curves for currents between 0.1 and 100 mA in single crystals. In Ref. 40, they have found that deviations from linearity start above 30 mA. Therefore, they have chosen a measuring current well below this value at 10 mA ($J \simeq 4.5$ \times A/cm²). As a consequence, although T_c is very robust to



FIG. 4. The temperature dependence of electrical resistivity of the (Hg,Re)-1223 sample for J=1.5 A/cm². The inset shows the T^* determined from fitting up to 200 K using J=0.7 A/cm².

these kind of current variations, it can occur an apparent discrepancy to define the pseudogap temperature T^* . According to Tallon and Loram,² when the resistivity measurement is plotted to 300 K, T^* is equal to 195 K, which is defined as the temperature which $\rho(T)$ goes under the linear regime as the temperature goes down. However, when the same resistivity data are plotted up to 600 K, a visual inspection yields T^* at 320 K.

As an example we show in Fig. 4 one of our typical resistivity measurements as a function of the temperature for $J=1.5 \text{ A/cm}^2$. As one can see through the inset, if we use a value of $J=0.7 \text{ A/cm}^2$, the value of T^* changes drastically. There are two factors responsible for such a discrepancy: one is the pure visual analysis that is a subject of great uncertainty and must be replaced by derivative analysis. The other is the different values of J. As we show below in Fig. 5, $J = 1.5 \text{ A/cm}^2$ is already in the nonlinear regime, and as a consequence, the according value of T^* is too high.

In general, the dependence of average voltage on the current can be written as the following expansion:



FIG. 5. Isotherms of the sample *B*. The symbol (\Box) denotes $V \times I$ curve at T=145 K and the symbol (\blacksquare) denotes $V \times I$ curve at T=170 K. The straight line is a linear regression fit and the dashed line represents a polynomial (second rank) fit.

$$V = R_1 I + R_2 I^2 + \cdots,$$
 (1)

where $R_1 = R_1(T)$ and $R_2 = R_2(T)$.

In Fig. 5 we plot the curves V=V(I) for only one of our samples since the curves for the others have the same features. This figure shows that, for T=170 K, V=V(I) is a linear function up to J=4.2 A/cm². However, for lower temperatures, nonlinear effects develop in the V(I) due to a nonvanishing value of R_2 . As displayed in Fig. 5, for T=145 K we have found that nonlinear behavior appears above J>1.04 A/cm². Thus, with the purpose of obtaining the high temperature linear behavior and the value of T^* accurately, one has to use $J \le 1$ A/cm² for sample *B*. Accordingly, the same analysis for sample *A* yields the maximum linear current J=1.05 A/cm² and for sample C, J=1.00 A/cm². Thus, in what follows, we have taken the data with J=1.0 A/cm² for our three samples.

Taking into account the above optimum density current value, which assures us that the systems are in the linear regime ($R_2=0$) for $T>T_c$, we can write that

$$R_1(T) = R_0 + \frac{\partial R}{\partial T}(T - T_0) + \frac{\partial^2 R}{\partial T^2}(T - T_0)^2 + \cdots, \qquad (2)$$

where T_0 is any chosen temperature in the range of T_c and shows that the resistivity is linear with the temperature whenever $\partial^2 R / \partial T^2 = 0$ and $\partial R / \partial T$ is independent of the temperature.

Therefore, we can determine the values of $T^{*}(n)$ analyzing the first $(\partial \rho / \partial T)$ and second $(\partial^2 \rho / \partial T^2)$ derivatives of the resistivity with respect to the temperature. The study of the regions, where the second derivative vanishes or changes sign, has been used recently by Ando et al.⁴¹ to investigate the pseudogap phase of many compounds. Furthermore, Nagib *et al.*¹⁶ have estimated T^* above and below T_c (by the use of Zn impurities) using the same method. They verified that for nearly identical values of a number of holes, both sintered and high oriented thin film of $Y_{1-x}Ca_xBa_2(Cu_{1-y}Zn_y)_3O_{7-\delta}$ have the same values of T^* . The only difference between polycrystalline samples and thin film is the residual resistivity value. The polycrystal has a residual resistivity due to the percolative effect and great contributions from the grain boundaries.

As mentioned, the resistivity must be analyzed at a low density of current to avoid the nonlinear regime. On the other hand, lower values of *J* are susceptible to high resistivity oscillations and do not allow an accurate estimation on T^* . Figures 6(a)-6(c) show $(d\rho/dT)/(d\rho/dT)_{T=170 \text{ K}}$ and $d^2\rho/dT^2$ for $J=1 \text{ A/cm}^2$. In these curves one can see that $(d\rho/dT)/(d\rho/dT)_{T=170 \text{ K}}$ varies as the temperature is reduced down to T_c but converges to a constant value as the temperature increases.

The graphical analysis yielded $T^* = (160 \pm 2)$ K for sample A, $T^* = (154 \pm 2)$ K for sample B, and $T^* = (151 \pm 2)$ K for sample C. The uncertainties were estimated in the interval where the $(d\rho/dT)/(d\rho/dT)_{170 \text{ K}}$ curves start to deviate from the background and in the range of temperature in which $d^2\rho/dT^2$ vanishes.



FIG. 6. The first and second derivative of resistivity with respect to the temperature for (a) sample A, (b) sample B, and (c) sample C. It was applied $J=1 \text{ A/cm}^2$. T_{scf} was defined from $d^2\rho/dT^2$ as the temperature at which strong and downturn in $\rho(T)$ becomes evident near T_c .

B. Superconducting fluctuations

As explained in the Introduction, one of the main proposals to the pseudogap phase is the existence of superconducting fluctuations without phase coherence.^{4,5} According to this

TABLE III. Comparison of the critical temperature, fluctuation conductivity, and pseudogap temperature.

Sample	$T_c(\mathbf{K})$	$T_{scf}(\mathbf{K})$	$T^*(K)$
A	132.6±0.2	139±1	160±2
В	133.2 ± 0.2	140 ± 1	155 ± 2
С	132.7 ± 0.2	139±1	151±2

scenario, the HTSC exhibit complex behavior, which is related to thermodynamic fluctuations of the superconducting order parameter. These fluctuations affect the electrical resistivity characteristics in normal phase.

For the polycrystalline samples case there are two models that can give a picture of fluctuations in intergrain and intragrain regions. The first model proposed by Aslamasov and Larkin⁴² is associated with fluctuations in intergrain and intragrain regions, however, the second developed by Lawrence and Doniach⁴³ can be applied only for a description of fluctuations into an intragrain region of a layered superconductor.

1. Aslamasov-Larkin model

The thermodynamic fluctuations near the transition were first studied by Ginzburg,⁴⁴ and these effects in type I superconductors were shown to be negligible in 1960. However, the Aslamasov and Larkin report⁴² has considered the effects of the superconducting fluctuations on the conductivity or paraconductivity to be non-negligible. Furthermore, the fluctuations are enhanced for sufficiently dirty films and whisker crystals.⁴² Recently Naqib et al.¹⁶ calculated the temperature where such fluctuations set in T_{scf} and concluded that it is distinct from T^* , because they respond differently to an applied magnetic field. It is clear that the presence of Cooper pairs will affect the electrical resistivity. Therefore, following Naqib and co-workers, we used the same set of resistivity data to determine T_{scf} and to estimate T^* using the onset of the vanishing of $d^2\rho/dT^2$ at a finite $d\rho/dT$.¹⁶ The results are displayed in Table III. The T_{scf} values have a similar behavior of T_c , which presented a different trend than that of T^* in agreement to Naqib et al.¹⁶

The paraconductivity is generally described by two contributions: $\Delta \sigma = \Delta \sigma_{AL} + \Delta \sigma_{MT}$. In the first, in the Aslamasov– Larkin (AL) framework,⁴² the excess conductivity $\Delta \sigma$ above T_c is derived using a microscopic approach by a mean field theory, which is considered a direct contribution to paraconductivity^{10,15} given by

$$\Delta \sigma_{AL}(\epsilon) = C \epsilon^{-\alpha} \tag{3}$$

with $\epsilon = (T - T_c)/T_c$ and

$$C = \frac{e^2}{16\hbar d}, \quad \alpha = 1 \quad \text{for 2D} \tag{4}$$

$$C = \frac{e^2}{32\hbar\xi_z(0)}, \quad \alpha = \frac{1}{2} \quad \text{for 3D.}$$
 (5)

Here α is the critical exponent related to the dimension of the fluctuations, $\xi_z(0)$ is the zero-coherence length in the z direc-



FIG. 7. Analysis of the excess conductivity normalized in logarithmic scale for sample *B*. The linear fitting indicates 3D $(\alpha = \frac{1}{2})$ and 2D $(\alpha = 1)$ regimes. The crossover temperature T_{LD} is also indicated by arrows.

tion for three-dimensional (3D) fluctuations, e is the electronic charge, and d is characteristic nonsuperconductor thickness between two superconductor layers. The second contribution arising from the pair-break interaction is known as an indirect anomalous Maki–Thompson (MT) contribution.^{45,46} Since the MT contribution is negligible in cuprate superconductors,¹⁶ only the AL contribution will be considered ($\Delta \sigma \cong \Delta \sigma_{AL}$).¹⁵

The evaluation of the AL conductivity contribution can be extracted from the slope of the $\Delta \sigma_{AL}$ versus ϵ logarithmic plot. The procedure is to fit, for all the three samples, the linear *T*-dependent resistivity $\rho_n = a + bT$ in the interval 220–270 K (see Fig. 4). For all cases, the excess conductivity $\Delta \sigma_{AL}$ was obtained by subtracting the measured conductivity $1/\rho(T)$ from the linear extrapolated normal-state conductivity $1/\rho_n(T)$:⁴⁷

$$\Delta \sigma_{AL} = \frac{1}{\rho(T)} - \frac{1}{\rho_n(T)}.$$
(6)

From Eq. (3) it can be shown that

$$\ln \frac{\Delta \sigma_{AL}}{\sigma_{270 \text{ K}}} = \ln \left(\frac{C}{\sigma_{270 \text{ K}}}\right) - \alpha \ln \epsilon.$$
(7)

Figure 7 shows the dependence of normalized excess conductivity for sample *B* in the form $\ln[\Delta \sigma_{AL}/\sigma_{270 \text{ K}}]$. The $\xi_z(0)$ and thickness *d* can be determined from the AL formula



FIG. 8. A particle model that is formed by a set of grains (lamellas). The particle can be defined as a linear sequence of edge dislocations of the grain growth. In our case, the grain is composed of (Hg,Re)-1223 phase (rich in oxygen) and Hg-1223 phase (poor in oxygen).

using the linear coefficients of the fit when $\alpha = \frac{1}{2}$ and 1 (see Table IV). The $\xi_{z}(0)$ and d values are relatively large as compared to texture, single crystal, and grain-aligned samples.^{10,48,49} These results can be understood with the aid of a simple grain model. Ceramic samples exhibit complex transport behavior because they are composed of particles, where there are grains with pores, microcracks, and stacking faults. Intergrain junctions establish the link between different particles, as can be seen in Fig. 2. We define a single crystal as a region where discordances are $\leq 5^{\circ}$ and grains as being a set of single crystals. As an example, a tilt boundary, which is formed from a linear sequence of edge dislocations (grain), is shown in Fig. 8(a). Each lamella in Fig. 8(a) represents a grain, and the grains together form an agglomeration that is named by particle. For instance, Fig. 8(b) shows up a particle formed by five grains (lamellas) that presents a thickness of \cong 4500 Å, although there are particles with six or seven lamellas, and the image contrast of one grain allowed us to identify three or four different tilts. We have observed that there are, in general, three single crystals inside each grain. Therefore, one single crystal was estimated to have an average size of 1500 Å. The analysis of Table IV

TABLE IV. Results for the zero-coherent length and distance between planes. The temperature T_{LD} is obtained by an intersection between linear fits from analysis of excess conductivity curves.

Sample	$\sigma_{\rm 270}~{\rm K}~(\Omega~{\rm cm})^{-1}$	$\xi_z(0)$ (Å)	d_{AL} (Å)	T_{LD} (K)	d_{LD} (Å)
A	10234	150	1460	143±1	287
В	29749	60	1290	140 ± 1	113
С	18833	80	1090	139±1	150

suggests that the thickness d can be interpreted as an average space between grains. Moreover, this intergrain region is formed by two Hg-1223 underdoped crystals, which are in agreement with the values l found in Table I for the Hg-1223 phase. In principle, this hypothesis can justify our superconducting-insulating-superconducting (SIS) junction type³¹ and the thickness d is larger than the finding in the grain-aligned Hg-1223 sample from Ref. 49.

2. Lawrence-Doniach model

Thus, the grain can be described as proposed in Fig. 8(c), and in the intragrain region, the Lawrence and Doniach (LD) model⁴³ can give an appropriate description of the fluctuations. For this model, superconducting layers are coupled by the Josephson effect and the variation of conductivity shows different temperature behavior for different dimensions.

Following the Schmidt formalism,⁵⁰ Lawrence and Doniach derived an expression for the fluctuation-induced inplane conductivity⁴³

$$\Delta \sigma_{LD} = \frac{e^2}{16\hbar d} \epsilon^{-1} \left[1 + \left(\frac{2\xi_z(0)}{d}\right)^2 \right]. \tag{8}$$

The LD model predicts that near T_c a crossover of the dimensionality of the fluctuations occurs and is given by

$$T_{LD} = T_c \left[1 + \left(\frac{2\xi_z(0)}{d} \right)^2 \right].$$
⁽⁹⁾

The Lawrence-Doniach approach suggests a change from 2D to 3D behavior at T_{LD} , which can be determined from our experimental data by extrapolation of straight lines and taking a crossover point. The change of slope shown in Fig. 7 indicates a crossover from 2D with $\alpha = 1$ to 3D with $\alpha = \frac{1}{2}$. Therefore, the resistivity points above $T_{LD}(n)$ in Fig. 7 are characterized by the 2D exponent $\alpha = 1$. The data below $T_{LD}(n)$ are characterized by the 3D exponent $\alpha = \frac{1}{2}$ indicating that in this temperature regime the single crystals are coupled.

From the Lawrence and Doniach framework one can assume that inside the grain (intragrain region) the nonsuperconductor region separates the superconducting layers, which is in agreement with the x-ray diffraction analysis where two phases were found: (Hg,Re)-1223 (rich in oxygen) and Hg-1223 (poor in oxygen). The single crystal average size evaluated to Hg-1223 phase, by x-ray diffraction with Rietveld refinement, are in agreement with the thickness obtained by the LD approach using T_{LD} , T_c , and $\xi_z(0)$ as input parameters (see Tables I and IV).

In our simple grain model, T_{LD} physically means that Josephson coupling is taking place between (Hg,Re)-1223 single crystals separated by Hg-1223 phase. In addition, there are indications that above T_c the Hg-1223 underdoped phase is an insulating barrier between (Hg,Re)-1223 single crystals, which present fluctuations effects.

Summarizing, the AL models provides $\xi_z(0)$ and *d* parameters, which are influenced by intergrain and intragrain regions; however, the Lawrence-Doniach model describes the effects caused from the intragrain fluctuation behavior.



FIG. 9. The (Hg,Re)-1223 phase diagram with values of T_c , T_{scf} , T_{LD}^{exp} , and T^* as a function of the charge carrier density. The straight line is drawn as a guide to the eye.

IV. DISCUSSIONS

In Fig. 9 we have presented the phase diagram T versus n, that is $T_c(n)$, $T_{scf}(n)$, $T_{LD}(n)$, and $T^*(n)$ for our compounds of the (Hg,Re)-1223 calculated by our resistivity data. We have used the values of $T_c(n)$ measured by the ac magnetic susceptibility χ_{ac} . As discussed above, the values of $T^*(n)$ are very subtle to be determined. Thus, our results and calculations were made only after a very careful analysis of the voltage-current [V(I)] isotherms with the purpose of investigating the best range of current density and temperature where V(I) is in the linear regime for our samples.

In order to verify the different nature among pseudogap temperature T^* , thermodynamic fluctuations temperature T_{scf} , and the dimensionality of the fluctuation at a temperature T_{LD} , we have performed an investigation about the fluctuation conductivity $\Delta \rho$. The results indicate that both $T_{LD}(n)$ and $T_{scf}(n)$ are distinct from $T^*(n)$. The $T_{scf}(n)$ curve follows the shape of $T_c(n)$, and the difference between T_{scf} and T_c is less than 7 K. These same trends were reported by Naqib *et* $al.^{16}$ and by Vidal *et al.*⁵¹ The low values of T_{scf} with respect to T^* do not favor the scenario of the fluctuation of Cooper pairs for the pseudogap phase⁴ as already criticized by Lee *et* $al.^5$

The phase diagram suggests that $T^*(n)$ is the onset of small superconducting islands that appeared due to the local charge inhomogeneity or local different oxygen content. Regions of different charge content have different local values of Tc,^{4–7} and these superconducting regions provide a physical interpretation to the downturn of the resistivity from the linear behavior below $T^*(n)$. This is also verified by susceptibility data, which are consistent with a magnetization signal at some region of each (Hg,Re)-1223 crystal. As discussed in ac magnetic susceptibility measurements, items near the T_c (Hg,Re)-1223 phase suffer fluctuation effects. However, in the Hg-1223 phase ($T_c \cong 124$ K) these effects are reduced and it can be considered an insulating phase (poor oxygen content). The cooling of the sample increases the size of this region, which is first 2D dimensionality and below T_{LD} it turns to 3D dimensionality. The T_c onset represents the point where the islands are big enough to promote percolation among grains and particles.

V. CONCLUSION

We have prepared samples of (Hg,Re)-1223 superconductors and developed a reliable method to study T^* through careful resistivity measurements, as explained above. Our aim is to gain some insight into the normal or pseudogap phase of these superconductors. In order to accomplish this task, we have calculated $T^*(n)$, $T_{LD}(n)$, $T_{scf}(n)$, and made a fine analysis together with previous results of $T_c(n)$.

From our results and the assumption that the HTSC are inhomogeneous materials,^{1,2,5} a possible scenario to normal phase is as follows: T^* is the onset of small superconducting islands that appeared due to the local charge inhomogeneity or local different oxygen content. Because of this disorder, samples composed of many inhomogeneous regions may form stripes or patchwork patterns.^{4–7} Initially these islands are isolated and therefore there is a decrease in the resistivity, as seen by the downturn from the linear regime, but it is still finite. As the temperature decreases, these islands grow and a new one appears, and there is some overlapping of superconducting regions between the superconducting layers. At T_{LD} the Josephson coupling among the superconducting (intragrain) layers and the system crosses from 2D over to 3D behavior. As the temperature goes down, the size of the superconducting regions increases. The superconducting regions are large enough to percolate, and the sign of this behavior is given by the values of T_{scf} which is just above T_c .¹⁶

Another possibility is as follows: T^* is the onset of phase separation,^{5–7} which is very likely to occur in HTSC. In this case T^* has nothing to do with the superconducting phase as proposed by Tallon *et al.*² and is in agreement with the zinc doped superconductors' thin films resistivity measurements.¹⁶ In this case the superconducting regions are formed just above T_{LD} and this temperature marks the onset of coupling among the superconducting layers. At temperatures below T_{LD} the scenario is the same as in the above paragraph. However, the values of the T^* related to phase segregation are very large at low doping values,^{1,2} going up to 800 K, while if the T^* is the onset of superconducting islands and it assumes much lower values, comparable to the Nernst temperature.⁵²

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