



PARAMAGNETIC SCATTERING OF NEUTRONS BY
RARE-EARTH IONS: CALCULATED PARAMAG-
NETIC CROSS SECTIONS FOR Ce, Pr, Nd, Gd,
Tb, Dy, Ho, Er, Tm and Yb.

MARIETA C. MATTOS



PUBLICAÇÃO IEA N.º **166**
Junho — 1968

INSTITUTO DE ENERGIA ATÔMICA
Caixa Postal 11049 (Pinheiros)
CIDADE UNIVERSITÁRIA "ARMANDO DE SALLES OLIVEIRA"
SÃO PAULO — BRASIL

PARAMAGNETIC SCATTERING OF NEUTRONS BY RARE-EARTH IONS:
CALCULATED PARAMAGNETIC CROSS SECTIONS FOR Ce, Pr, Nd,
Gd, Tb, Dy, Ho, Er, Tm and Yb.*

Marieta C. Mattos

Divisão de Física Nuclear
Instituto de Energia Atômica
São Paulo - Brasil

Publicação IEA Nº 166
Junho - 1968

Comissão Nacional de Energia Nuclear

Presidente: Prof. Uriel da Costa Ribeiro

Universidade de São Paulo

Reitor: Prof. Dr. Luis Antonio da Cama e Silva

Instituto de Energia Atômica

Diretor: Prof. Rômulo Ribeiro Pieroni

Conselho Técnico-Científico do IEA

Prof. Dr. José Moura Gonçalves	}	pela USP
Prof. Dr. José Augusto Martins		
Prof. Dr. Rui Ribeiro Franco	}	pela CNEN
Prof. Dr. Theodoretto H. L. de Arruda Souto		

Divisões Didático-Científicas

Divisão de Física Nuclear -
Chefe: Prof. Dr. Marcello D. S. Santos

Divisão de Radioquímica -
Chefe: Prof. Dr. Fausto Walter de Lima

Divisão de Metalurgia Nuclear -
Chefe: Prof. Dr. Tharcísio D. S. Santos

Divisão de Engenharia Química -
Chefe: Lic. Alcídio Abrão

Divisão de Radiobiologia -
Chefe: Prof. Dr. Rômulo Ribeiro Pieroni

Divisão de Engenharia Nuclear -
Chefe: Engº Pedro Bento de Camargo

Divisão de Operação e Manutenção de Reatores -
Chefe: Engº Azor Camargo Penteado Filho

Divisão de Física de Reatores -
Chefe: Prof. Paulo Saraiva de Toledo

Divisão de Ensino e Formação -
Chefe: Prof. Dr. Rui Ribeiro Franco

PARAMAGNETIC SCATTERING OF NEUTRONS BY RARE-EARTH IONS:
CALCULATED PARAMAGNETIC CROSS SECTIONS FOR Ce, Pr, Nd,
Gd, Tb, Dy, Ho, Er, Tm and Yb.*

Marieta C. Mattos

RESUMO

A teoria dada por Trammell foi usada para se calcular a secção de choque total de espalhamento paramagnético de nêutrons para os ions de terras raras. Os fatores de forma magnéticos foram calculados usando-se as funções determinadas por Blume, Freeman e Watson, assumindo-se funções de onda de Hartree-Fock.

RESUMÉ

La théorie donnée par Trammell a été employée pour calculer la section efficace totale de diffusion paramagnétique des neutrons par les ions des terres rares. Les facteurs de forme magnétiques ont été calculés utilisant les fonctions déterminées par Blume, Freeman et Watson, en supposant des fonctions d'onde de Hartree-Fock.

ABSTRACT

The theory given by Trammell has been used for calculating the total paramagnetic scattering cross section of neutrons for rare-earth ions. The magnetic form factors have been calculated using the functions determined by Blume, Freeman and Watson, assuming Hartree-Fock wave-functions.

* Reprinted from The Journal of Chemical Physics, Vol. 48, nº 1, 520-522, 1 January 1968.

Paramagnetic Scattering of Neutrons by Rare-Earth Ions: Calculated Paramagnetic Cross Sections for Ce, Pr, Nd, Gd, Tb, Dy, Ho, Er, Tm, and Yb

MARIETA C. MATTOS

*Nuclear Physics Division, Instituto de Energia Atômica,
 São Paulo, Brazil*

(Received 3 July 1967)

The theory given by Trammell¹ for the paramagnetic scattering of neutrons by rare-earth ions has been used.

The total paramagnetic cross section is given by^{1,2}

$$\sigma_{pm} = \frac{2}{3}\pi (e^2/mc^2)^2 \gamma^2 \mu^2 \bar{f}^2,$$

where e^2/mc^2 is the classical electronic radius, γ and μ are the magnetic moments of the neutron and of the atom, respectively, and \bar{f}^2 is the average over all scattering angles of the squared magnetic form factor.

The form factors were calculated assuming Hund ground state and Russell-Saunders coupling for the 4f electrons. The functions determined by Blume, Freeman, and Watson,³ assuming Hartree-Fock wavefunctions were used for evaluating the orbital and spin contributions. For Pm, Sm, and Eu, the form factors

have not been calculated because of the narrowness of the multiplet spacings and of contributions of J states other than the lowest⁴⁻⁶ so that the assumption of Hund ground state is no longer valid. In this assumption there is no paramagnetic scattering for Eu. Since Gd³⁺ is in an S state, there is just the spin contribution to its form factor.

Table I gives the values of \bar{f}^2 as a function of wavelength, calculated by numerical integration for the rare earths. \bar{f}^2 reduces to unity for wavelengths large compared to the linear size of the 4f electron distribution and approaches zero for wavelengths comparable to the diameter of the 4f shell. Figure 1 shows the calculated curves of \bar{f}^2 for Nd³⁺ and Gd³⁺, corresponding, respectively, to form factors having the largest and no orbital contribution. The other curves fall between these two.

For the calculation of σ_{pm} the measured values of the

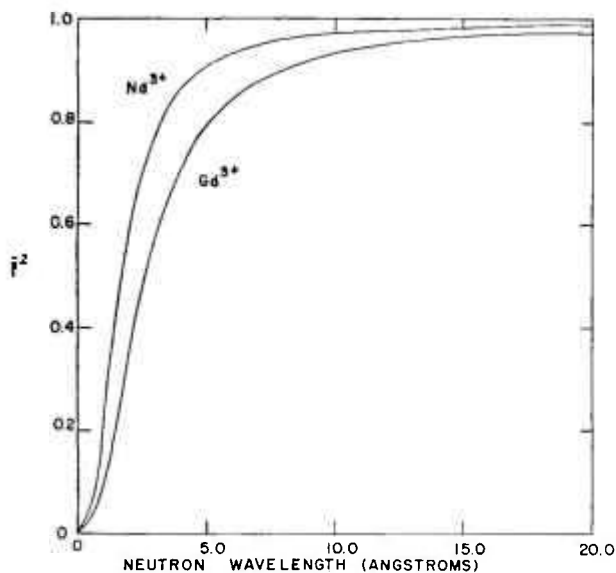


FIG. 1. Average squared magnetic form factors for Nd³⁺ and Gd³⁺.

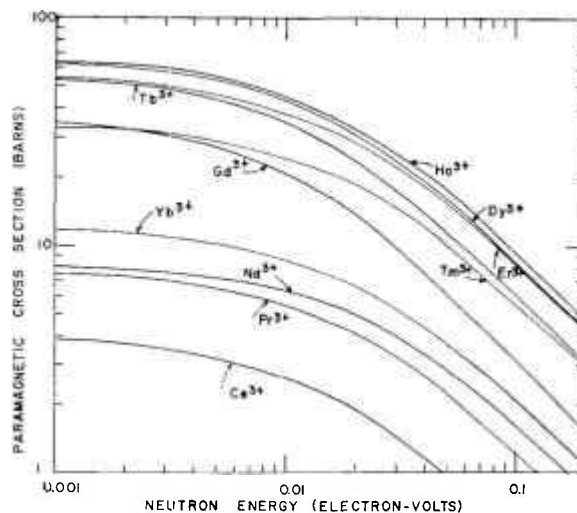


FIG. 2. Calculated total paramagnetic cross sections.

TABLE I. Values of f^2 as a function of wavelength.

λ (Å)	Ce ³⁺	Pr ³⁺	Nd ³⁺	Gd ³⁺	Tb ³⁺	Dy ³⁺	Ho ³⁺	Er ³⁺	Tm ³⁺	Yb ³⁺
20.00	0.980	0.984	0.988	0.972	0.964	0.979	0.980	0.982	0.983	0.984
10.00	0.951	0.961	0.972	0.933	0.937	0.949	0.953	0.957	0.960	0.962
5.00	0.849	0.877	0.909	0.797	0.825	0.844	0.856	0.866	0.873	0.880
2.86	0.646	0.701	0.764	0.554	0.607	0.641	0.656	0.683	0.698	0.712
2.00	0.466	0.521	0.596	0.357	0.416	0.454	0.478	0.505	0.524	0.541
1.54	0.327	0.379	0.449	0.231	0.283	0.318	0.342	0.367	0.386	0.403
1.25	0.232	0.275	0.334	0.155	0.196	0.230	0.246	0.267	0.283	0.299
1.00	0.154	0.185	0.230	0.099	0.128	0.152	0.164	0.180	0.193	0.206
0.87	0.117	0.142	0.177	0.075	0.097	0.116	0.126	0.138	0.149	0.159
0.74	0.085	0.103	0.130	0.055	0.070	0.084	0.091	0.101	0.109	0.116

magnetic moments⁷ of the rare-earth ions in the form of oxide have been used. Figure 2 shows the calculated total paramagnetic cross sections of the rare earths as a function of energy. The curves for Pr, Ho, Er, Tm, and Yb have already been published⁸ and are presented here for completeness.

The agreement verified in the comparison⁸ of calculated and experimental form factors for Ho³⁺ and Tm³⁺ indicates that the calculated total paramagnetic cross sections presented in Fig. 2 for the rare-earth ions can be used in the analysis of data obtained by total neutron cross-section measurements.

¹ G. T. Trammell, Phys. Rev. **92**, 1387 (1953).

² O. Harper and M. H. Johnson, Phys. Rev. **55**, 898 (1939).

³ M. Blume, A. J. Freeman, and R. E. Watson, J. Chem. Phys. **37**, 1245 (1962); **41**, 1878 (1964).

⁴ D. M. Yost, H. Russell, Jr., and C. S. Garner, *The Rare Earth Elements and Their Compounds* (John Wiley & Sons, Inc., New York, 1950), Chap. 2.

⁵ K. A. Gschneidner, Jr., *Rare Earth Alloys* (D. Van Nostrand Co., Inc., New York, 1961), p. 43.

⁶ J. H. Van Vleck, *The Theory of Electric and Magnetic Susceptibilities* (Oxford University Press, London, 1932), p. 245.

⁷ J. A. Gibson and G. S. Harvey, "Properties of the Rare Earth Metals and Compounds," Tech. Rept. AFML-TR-65-430, January 1966.

⁸ R. L. Zimmerman, L. Q. Amaral, R. Fulfarò, M. C. Mattos, M. Abreu, and R. Stasiulevicius, Nucl. Phys. **A95**, 683 (1967).